

21ST INTERNATIONAL LINGUISTICS OLYMPIAD

Team problem – Lexicostatistics

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Manual procedure

	Toba	Pilagá	Mocoví	Kadiwéu
cloud	l=ʔok ₁	ʔo=ʔok ₁	naweyek ₂	lol:adi ₃
fire	nodek ₁	ʔd=oleʔ ₂	norek ₁	n=ol:edi ₂
fish	njaq ₁	ʔnijaq ₁	naʔin ₂	nij:ogo-dʒegi ₃
head	=qajk ₁	=qajk ₁	=qaik ₁	=ak:ilo ₂
to kill	=alawat ₁	=aʔa:t ₁	=alawat ₁	=el:owadi ₁
moon	ʔawoʔojk ₁	ʔaʔwoʔojk ₁	firaʔyo ₂	ep:enaj ₃
nose	=mik ₁	=ʔmik ₁	=mik ₁	=m:iq:o ₁
salt	towe ₁	olʔyek ₂	ʔwe ₁	jok:i ₋₁
stone	qaʔ ₁	ʔqaʔ ₁	qaʔ ₁	wet:iɡa ₂
tongue	=aʔf-arat ₁	=aʔf-aʔat ₁	=oʔleʔ-aran-arat ₂	=ok:el:i ₃

	Toba	Pilagá	Mocoví	Kadiwéu	
cloud	1	1	2	3	2/4
fire	1	2	1	2	2/4
fish	1	1	2	3	2/4
head	1	1	1	2	3/4
to kill	1	1	1	1	4/4
moon	1	1	2	3	2/4
nose	1	1	1	1	4/4
salt	1	2	1	-1	2/3
stone	1	1	1	2	3/4
tongue	1	1	2	3	2/4

	Toba	Pilagá	Mocoví
Pilagá	8/10 = 0.80	–	–
Mocoví	6/10 = 0.60	4/10 = 0.40	–
Kadiwéu	2/9 = 0.22(2)	3/9 = 0.33(3)	2/9 = 0.22(2)

Borrowings (indicated by negative indices) are ignored in the manual procedure for all purposes.

Assignment I. Stability indices: maximum number of languages using cognate roots divided by total number of languages that have a native (non-borrowed) root.

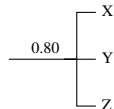
Manual procedure – Algorithm A vs. Algorithm B

Assignment K. When clustering, Algorithm A uses the minimum value, Algorithm B uses the average.

Assignment J. Lexicostatistical distance: number of cognates divided by total number of comparable (non-borrowed) items. The maximum value during each iteration makes it to the tree, and the respective lects are grouped under a node. A new value is assigned to the node (see assignment K).

	Toba	Pilagá	Mocoví
Pilagá	8/10 = 0.80	–	–
Mocoví	6/10 = 0.60	4/10 = 0.40	–
Kadiwéu	2/9 = 0.22(2)	3/9 = 0.33(3)	2/9 = 0.22(2)

	X	Y	...
Y	0.80	–	–
Z	0.80	0.80	–
...

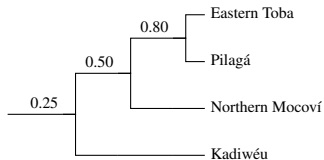
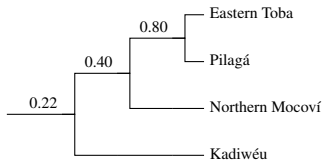


Toba + Pilagá = 0.80	Toba + Pilagá	Mocoví
	min(0.60; 0.40) = 0.40	
	min(0.22(2); 0.33(3)) = 0.22(2)	0.22(2)

Toba + Pilagá = 0.80	Toba + Pilagá	Mocoví
	ave(0.60; 0.40) = 0.50	
	ave(0.22(2); 0.33(3)) = 0.27(7)	0.22(2)

[Toba + Pilagá] + Mocoví = 0.40	[Toba + Pilagá] + Mocoví
	min(0.22(2); 0.22(2)) = 0.22(2)

[Toba + Pilagá] + Mocoví = 0.50	[Toba + Pilagá] + Mocoví
	ave(0.27(7); 0.22(2)) = 0.25



Automated procedure

	Toba	Pilagá	Mocoví	Kadiwéu
cloud	l=ʔok ₁	'lo=ʔok ₁	naweyelek ₂	lol:adi ₃
fire	nodek ₁	'd=oleʔ ₂	norek ₁	n=ol:edi ₂
fish	njaq ₁	'nijaq ₁	na.ɫin ₂	nij:ogo-dʒeg ₃
head	=qajk ₁	'=qajk ₁	=qaik ₁	=ak:ilo ₂
to kill	=alawat ₁	=a'la:t ₁	=alawat ₁	=el:owadi ₁
moon	ʔawoʋojk ₁	ʔa'woʋojk ₁	firajyo ₂	ep:enaj ₃
nose	=mik ₁	'=mik ₁	=mik ₁	=m:iq:o ₁
salt	towe ₁	ol'ʒek ₂	ʔwe ₁	jok:i- ₁
stone	qaʔ ₁	'qaʔ ₁	qaʔ ₁	wet:iga ₂
tongue	=atʃ-awat ₁	=a'tʃ-aʃat ₁	=oʔley-awan-awat ₂	=ok:eli ₃

	Toba	Pilagá	Mocoví	Kadiwéu	
cloud	HK	HK	NK	RR	2/4
fire	NT	HR	NR	HR	2/4
fish	NK	NK	NR	NK	3/4
head	KK	KK	KK	HK	3/4
to kill	HR	HR	HR	HR	4/4
moon	HK	HK	SR	HP	2/4
nose	MK	MK	MK	MK	4/4
salt	TH	HR	HH	YK	1/4
stone	KH	KH	KH	WT	3/4
tongue	HS	HS	HR	HK	2/4

	Toba	Pilagá	Mocoví
Pilagá	8/10 = 0.80	–	–
Mocoví	4/10 = 0.40	4/10 = 0.40	–
Kadiwéu	3/10 = 0.30	4/10 = 0.40	2/10 = 0.20

1) naweyelek → NK

2) ʔwe → HH

3) XY → Y:

=a $\boxed{\widehat{tʃ}}$ -awat → H \boxed{S}

P p b ɓ ɸ β f v

T t d ɗ θ ðð ʈ ɖ

S s z ʃ ʒ ʂ ʐ c ɟ

Y j ɟ (root-initially)

W w ɯ (root-initially)

H ɦ ʕ ɥ ʔ h ɦ ʔ, vowels,

and j ɟ w ɯ (except root-initially)

M m ɱ

N n ɳ ɲ ɳ

Q $\widehat{tʃ}$ $\widehat{dʒ}$

R r r l ʈ ʑ ʎ ʌ ʔ

K k g x ɣ q ɠ ɣ

Automated procedure – Algorithm A vs. Algorithm B

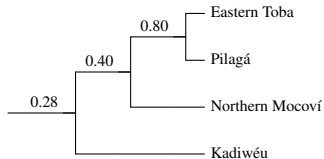
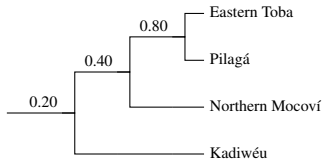
	Toba	Pilagá	Mocoví
Pilagá	$8/10 = 0.80$	–	–
Mocoví	$4/10 = 0.40$	$4/10 = 0.40$	–
Kadiwéu	$3/10 = 0.30$	$4/10 = 0.40$	$2/10 = 0.20$

Toba + Pilagá = 0.80	Toba + Pilagá	Mocoví
Mocoví	$\min(0.40; 0.40) = 0.40$	
Kadiwéu	$\min(0.30; 0.40) = 0.30$	0.20

Toba + Pilagá = 0.80	Toba + Pilagá	Mocoví
Mocoví	$\text{ave}(0.40; 0.40) = 0.40$	
Kadiwéu	$\text{ave}(0.30; 0.40) = 0.35$	0.20

[Toba + Pilagá] + Mocoví = 0.40	[Toba + Pilagá] + Mocoví
Kadiwéu	$\min(0.30; 0.20) = 0.20$

[Toba + Pilagá] + Mocoví = 0.40	[Toba + Pilagá] + Mocoví
Kadiwéu	$\text{ave}(0.35; 0.20) = 0.275$



Assignment A. Consonant class Ɂ.

	Toba	Pilagá	Mocoví	Kadiwéu
cloud	l=ʔok ₁	'lo=ʔok ₁	naweyelek ₂	lol:adi ₃
fire	nodek ₁	'd=oleʔ ₂	norek ₁	n=ol:edi ₂
fish	njaq ₁	'nijaq ₁	naʎin ₂	nij:ogo-ḏʒegi ₃
head	=qajk ₁	=qajk ₁	=qaik ₁	=ak:ilo ₂
to kill	=alawat ₁	=a'la:t ₁	=alawat ₁	=el:owadi ₁
moon	ʔawoʋojk ₁	ʔa'woʎojk ₁	firaɣo ₂	ep:enaj ₃
nose	=mik ₁	=mik ₁	=mik ₁	=m:iq:o ₁
salt	towe ₁	ol'ɣek ₂	ʔwe1	jok:i- ₁
stone	qaʔ ₁	'qaʔ ₁	qaʔ ₁	wet:iɣa ₂
tongue	=atʃ-awat ₁	=a'tʃ-aʔat ₁	=oʔleɣ-awan-awat ₂	=ok:el:i ₃

$$0.80 = 8/10$$

But...

ʔa'woʎojk → HK

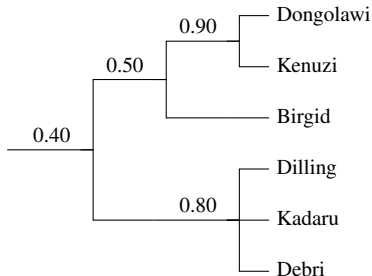
ʔawoʋojk (if Ɂ ∉ H) / ʔawoʎojk (if Ɂ ∈ H) → HK

Then, Ɂ belongs to consonant class **K** (or **H**, which is less likely, as Ɂ is known to be articulated at the back of the tongue).

Assignments B, C. Other Algorithm A trees for Nubian.

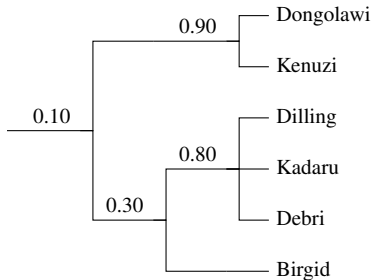
Assignment B.

Manual tree, Algorithm A.



Assignment C.

Automated tree, Algorithm A.

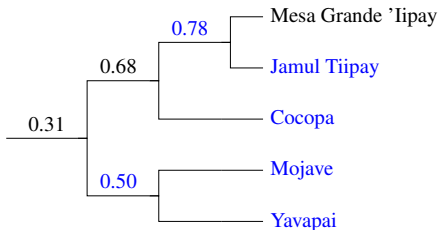


Assignment D. $0.491(6) = 59/120 = \text{ave}(\text{ave}(0.45; 0.45; 0.55); 0.50)$.

Assignments F, G.

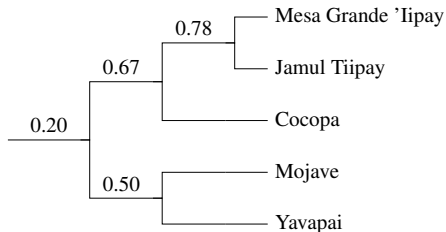
Assignment F.

Manual tree, Algorithm B.



Assignment G.

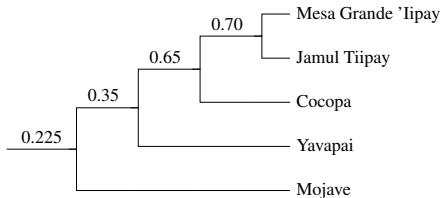
1. Distance = 0.20. Manual tree, Algorithm A.



Assignments G, H.

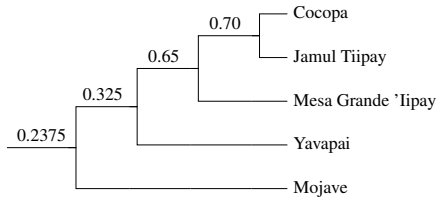
Assignment G.

2. Distance = 0.23. Automated tree,
Algorithm B.



Assignments G, H.

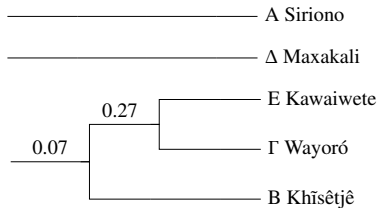
3. Distance = 0.24 = **0.2375**. Automated tree,
Algorithm B.



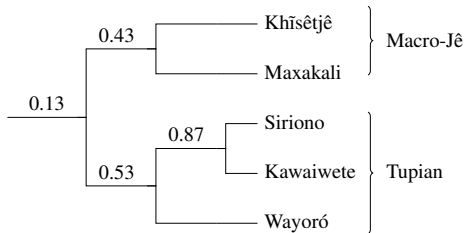
Assignment H. $0.2375 = \text{ave}(0.175; 0.30)$.

Assignment L.

Automated tree, Algorithm A.



Manual tree, Algorithm A.



A	B	Γ	Δ	E
Siriono	Khīsētjê	Wayoró	Maxakali	Kawaiwete

How did we check the correctness of the task?

```
Distance matrix for Nubian.txt
0.9
0.5 0.4
0.5 0.4 0.8
0.6 0.5 0.8 0.8
0.6 0.5 0.5 0.5 0.5
stability indeces [0.5, 0.8333333333333334, 1.0, 1.0, 0.5, 0.5, 0.8333333333333334, 0.8333333333333334, 0.8333333333333334, 0.5]
=====
Manual trees creation:
=====
Max value = 0.9
Number of max values = 1
Merge [Dongolawi + Kenuzi] with distance 0.9
=====
Max value = 0.8
Number of max values = 3
Merge [Kadaru + Deбри + Dilling] with distance 0.8
=====
Max value = 0.55
Number of max values = 1
Merge [[Dongolawi + Kenuzi] + Birgid] with distance 0.55
=====
Max value = 0.4916666666666667
Number of max values = 1
Merge [[[Dongolawi + Kenuzi] + Birgid] + [Kadaru + Deбри + Dilling]] with distance 0.4916666666666667
```

**Thank you for
your attention!**